

Shih Chien University

STP Program (July 01-Aug 02)

MATH 220 Differential Equations and Linear Algebra

Course Outline

Course Code: MATH 220

Instructor: TBA

Home Institution: TBA

Office Hours: TBA

Email: TBA

Credits: 4

Class Hours:

This course will have 144 class hours, including 50 lecture hours, professor 30 office hours, 20-hour TA discussion sessions, 10-hour review sessions, 34-hour extra classes.

Course Description:

This is a hybrid course that introduces basic concepts of linear algebra and differential equations. These two topics (put together) provide a very important toolkit for modeling real-world phenomena in science, engineering, business, etc. The course will cover linear algebra concepts such as vector spaces, linear dependence and independence, matrices, eigenvalues and eigenvectors, etc., and differential equation topics such as: uniqueness and existence of solutions to differential equations, first order equations, second order homogeneous and non-homogeneous equations, higher order equations, linear systems of differential equations, the heat equation and applications of differential equations.

Prerequisite: Calculus II



Course Objectives:

The major objective of this course is to introduce students to the basic concepts of linear algebra, differential equations, and applications of differential equations. Students will be expected to understand the basic concepts of differential equations well enough to be able to decide when, how, and why to apply them to real-world phenomena and to be able to interpret and communicate the results. This course is designed to help students progress in developing analytical thinking, critical reasoning, problem-solving, and communication skills. The goal is to obtain a useful mastery of basic concepts and methods to fully understand and appreciate the theory and practice of differential equations. Additionally, the course is expected to prepare students for studies in other disciplines in the sciences, engineering, business, etc.

Modality:

Online asynchronous. All lectures are pre-recorded and are made available on day one. Homework assignments are online (via WebAssign). The two exams (midterm and final, 1 hour 15 minutes each) will be proctored via zoom. You are supposed to have a webcam with a wide view capturing you and the entire desk.

Required Course Materials:

1) *Linear Algebra and Its Applications*, Fifth edition, by David C. Lay, Steven Lay, Judy McDonald Pearson, 2016.

Please do not buy this book before coming to class. The instructor will provide a direct link to the publisher's My Lab site, where you can get it with a discount as well as with an access to the online homework assignments.

2) Willian E. Boyce, Richard C. DiPrima: Elementary Differential Equations and Boundary Value Problems, 11th edition, Wiley, 2018.

Please do not buy this book before coming to class. The instructor will provide a direct link to the publisher's WileyPlus site, where you can get it with a discount as well as with an access to the online homework assignments.

Homework: There will be online WebAssign homework assignments for each section of the text. Each assignment will be made available on several days before the section is covered in class. The due date for each assignment will be set by your instructor and will generally be two or three days after the material is covered in class. You will get five attempts for each



Grading & Evaluation:

Attendance and participation:	10%
Homework:	30%
Midterm:	30%
Final:	30%

Grading System (1 ~ 100):

Quality Points	Grade	Percentage %
4	Α	80-100
3	В	70-79
2	С	60-69
1	D	50-59
0	E	0-49

Course Schedule

Week1 *Linear Algebra*: Introduction, linear systems, matrices, Gaussian elimination, reduced row echelon form, matrix operations, matrix inverses, determinants.

Week2 *Linear Algebra*: vector spaces, linear combinations, span and independence, subspaces, bases and dimension.

Week3 *Differential Equations*: Existence and uniqueness of solutions, first order linear, separable, exact, Bernoulli equations. Modeling with ordinary differential equations.

Week4 *Differential Equations*: Second order homogeneous and nonhomogeneous equations, mass-spring problem, and higher order equations. Laplace transforms and solutions of initial value problems. Power series solutions of differential equations.

Week5 *Differential Equations*: Systems of linear ordinary differential equations. Fourier series and introduction to partial differential equations (heat equation).



Detailed Course Outline:

Week		Chapter	Торіс
	1	Linear Algebra	1.1 Introduction
			1.2 Linear systems
			1.3 Matrices
			1.3 Matrix operations
1			1.4 Gaussian elimination
			1.5 Reduced row echelon form
			1.6 Matrix determinants and inverses
			1.7 Eigenvalues and eigenvectors
	2	Linear Algebra	2.1 Vector spaces
			2.2 Linear combinations
			2.3 Span
2			2.4 Linear independence
			2.5 Subspaces
			2.6 Basis and dimension
			Exam 1
			3.1 Existence and uniqueness of solutions
			3.2 First order linear and separable equations
3	3	First order ordinary	3.3 Exact and homogeneous first order
		differential equations	equations
			3.4 Special integrating factor, substitutions and
			Bernoulli equations
			3.5 Modeling with first order differential
			equations
			4.1 Homogeneous equations
			4.2 Non-homogeneous equations

4	4 Second and	4.3 Mass-spring problem
	higher order	4.4 Higher order equations



		ordinary differential equations	
			4.5 Laplace transforms and solutions of IVPs4.6 Power series solution on IVPs
			Exam 2
	5	Systems of linear differential equations	5.1 Systems of linear ordinary differential equations
5	6	Partial differential equations	6.1 Fourier series6.2 Introduction to partial differential equations (heat equation)
			Final Exam Discussion of final exam

Student responsibilities/expectations: The main course material will be presented through lectures. A discussion session, to be held every Friday will offer an opportunity for students to discuss course material and assigned problems with a teaching assistant (TA). Students are advised to keep pace with the course material as it is being presented. Consequently, students should endeavor to attend class and discussion sessions, and spend sufficient time working on assigned homework problems. If for any reason a student misses a class, he/she should endeavor to obtain the notes and learn the missed material. Students should not hesitate to ask questions or seek additional assistance to ensure that they are staying on pace with the class.

Examinations: There will be two midterm exams plus one cumulative final exam. The exams will contain problems to solve and definitions, brief explanations of concepts, and simple proofs.